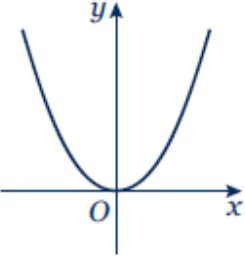


Examples - Sketching Quadratic Graphs

Key points

- The graph of the quadratic function $y = ax^2 + bx + c$, where $a \neq 0$, is a curve called a parabola.
- Parabolas have a line of one symmetry.
- To find where the curve intersects the y -axis substitute $x = 0$ into the function.
- To find where the curve intersects the x -axis substitute $y = 0$ into the function.
- At the turning points of a graph the gradient of the curve is 0 and any tangents to the curve at these points are horizontal.
- To find the coordinates of the maximum or minimum point (turning points) of a quadratic curve (parabola) you can use the completed square form of the function.

Example 1 Sketch the graph of $y = x^2$.

	The graph of $y = x^2$ is a parabola. When $x = 0$, $y = 0$. $a = 1$ which is greater than  zero, so the graph has the shape:
--	---

Example 2 Sketch the graph of $y = x^2 - x - 6$.

When $x = 0$, $y = 0^2 - 0 - 6 = -6$
So the graph intersects the y -axis at

$(0, -6)$

When $y = 0$, $x^2 - x - 6 = 0$

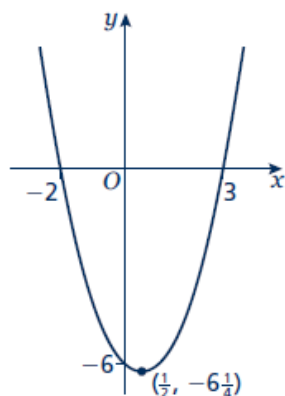
$$(x + 2)(x - 3) = 0$$

$$x = -2 \text{ or } x = 3$$

So,
the graph intersects the x -axis at $(-2, 0)$ and $(3, 0)$

$$\begin{aligned} x^2 - x - 6 &= \left(x - \frac{1}{2}\right)^2 - \frac{1}{4} - 6 \\ &= \left(x - \frac{1}{2}\right)^2 - \frac{25}{4} \end{aligned}$$

When $\left(x - \frac{1}{2}\right)^2 = 0$, $x = \frac{1}{2}$ and $y = -\frac{25}{4}$,
so the turning point is at the point $\left(\frac{1}{2}, -\frac{25}{4}\right)$



1 Find where the graph intersects the y -axis by substituting $x = 0$.

2 Find where the graph intersects the x -axis by substituting $y = 0$.

3 Solve the equation by factorising.

4 Solve $(x + 2) = 0$ and $(x - 3) = 0$.

5 $a = 1$ which is greater than  zero, so the graph has the shape:

6 To find the turning point, complete the square.

7 The turning point is the minimum value for this expression and occurs when the term in the bracket is equal to zero.