

Please check the examination details below before entering your candidate information

Candidate surname

Other names

**Pearson Edexcel
Level 3 GCE**

Centre Number

--	--	--	--	--

Candidate Number

--	--	--	--	--

Mock Paper

(Time: 2 hours)

Paper Reference **9MA0/01**

Mathematics

Advanced

Paper 1: Pure Mathematics 1

You must have:

Mathematical Formulae and Statistical Tables, calculator

Total Marks

Candidates may use any calculator allowed by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 15 questions in this question paper. The total mark for this paper is 100.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

S63448A

©2019 Pearson Education Ltd.

1/1/1/1/1/



Pearson

1.

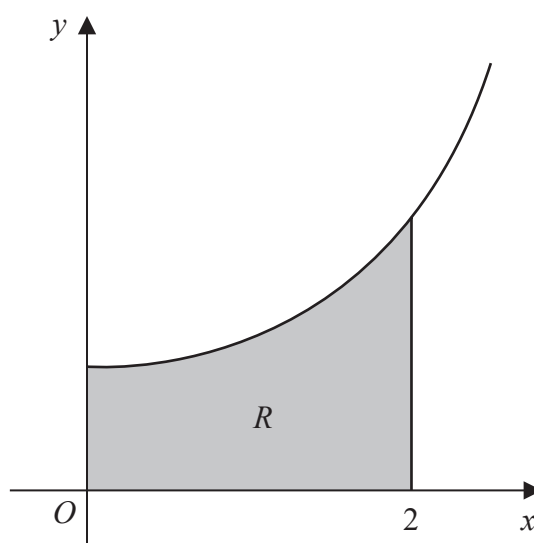


Figure 1

Figure 1 shows part of the curve with equation $y = e^{\frac{1}{5}x^2}$ for $x \geq 0$

The finite region R , shown shaded in Figure 1, is bounded by the curve, the y -axis, the x -axis, and the line with equation $x = 2$

The table below shows corresponding values of x and y for $y = e^{\frac{1}{5}x^2}$

x	0	0.5	1	1.5	2
y	1	$e^{0.05}$	$e^{0.2}$	$e^{0.45}$	$e^{0.8}$

- (a) Use the trapezium rule, with all the values of y in the table, to find an estimate for the area of R , giving your answer to 2 decimal places.

(3)

- (b) Use your answer to part (a) to deduce an estimate for

(i) $\int_0^2 (4 + e^{\frac{1}{5}x^2}) dx$

(ii) $\int_1^3 e^{\frac{1}{5}(x-1)^2} dx$

giving your answers to 2 decimal places.

(2)



Question 1 continued

Lined area for writing the answer to Question 1.

(Total for Question 1 is 5 marks)



DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

The points A , O and C lie on a straight line with $AO = 7.5$ cm and $OC = 8.5$ cm.

The size of angle AOB is 1.2 radians.

Find, in cm, the perimeter of the shape $AOCBA$, giving your answer to one decimal place.

(5)

Question 2 continued

Lined area for writing the answer to Question 2.

(Total for Question 2 is 5 marks)



3. The equation

$$3x^2 + k = 5x + 2 \quad k \in \mathbb{R}$$

where k is a constant, has no real roots.

Find the range of possible values for k .

(4)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Question 3 continued

Lined area for writing the answer to Question 3.

(Total for Question 3 is 4 marks)



DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

- DO NOT WRITE IN THIS AREA**

- DO NOT WRITE IN THIS AREA**

- DO NOT WRITE IN THIS AREA**

DO NOT WRITE IN THIS AREA

Question 4 continued

Lined area for writing the answer to Question 4.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



S 6 3 4 4 8 A 0 9 4 8

Question 4 continued

Lined area for writing the answer to Question 4.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Question 4 continued

Lined area for writing the answer to Question 4.

(Total for Question 4 is 10 marks)



5. A curve has equation

$$y = 4x^2 - 5x$$

The curve passes through the point $P(2, 6)$

Use differentiation from first principles to find the value of the gradient of the curve at P .

(5)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Question 5 continued

Handwriting practice area with 25 horizontal lines.

(Total for Question 5 is 5 marks)



6.

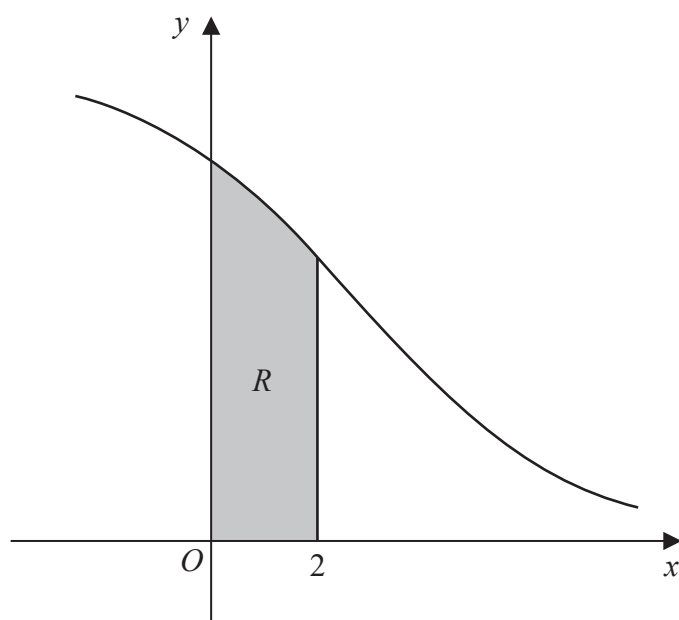


Figure 3

Figure 3 shows a sketch of part of the curve with equation

$$y = \frac{6}{e^{\frac{1}{2}x} + 4} \quad x \in \mathbb{R}$$

The finite region R , shown shaded in Figure 3, is bounded by the curve, the y -axis, the x -axis, and the line with equation $x = 2$

- (a) Use the substitution $u = e^{\frac{1}{2}x}$ to show that the area of R can be given by

$$\int_a^b \frac{12}{u(u+4)} du$$

where a and b are constants to be found.

(3)

- (b) Hence use algebraic integration to show that the exact area of R is $3 \ln \left(\frac{5e}{e+4} \right)$

(5)



Question 6 continued

Handwriting practice area with 25 horizontal lines.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Question 6 continued

Lined area for writing the answer to Question 6.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Question 6 continued

Lined area for writing the answer to Question 6.

(Total for Question 6 is 8 marks)



7. (a) Express $3 \sin \theta - 4 \cos \theta$ in the form $R \sin(\theta - \alpha)$, where $R > 0$ and $0 < \alpha < 90^\circ$. State the value of R and give the value of α to 2 decimal places.

(3)

The temperature in a greenhouse, $G^{\circ}\text{C}$, is modelled by the equation

$$G = 17 + 3 \sin(15t)^\circ - 4 \cos(15t)^\circ \quad 0 \leq t \leq 17$$

where t is the time in hours after 5 a.m.

- (b) Find, according to this model,

- (i) the maximum temperature in the greenhouse,

(1)

- (ii) the time, after midday, when the temperature in the greenhouse is 20°C .
Give your answer to the nearest minute.

(Solutions based entirely on graphical or numerical methods are not acceptable.)

(4)



Question 7 continued

Lined area for writing the answer to Question 7.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



S 6 3 4 4 8 A 0 1 9 4 8

Question 7 continued

Lined area for writing the answer to Question 7.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Question 7 continued

Lined area for writing the answer to Question 7.

(Total for Question 7 is 8 marks)



8. (i) Show that $y^2 - 4y + 7$ is positive for all real values of y .

(2)

(ii) Bobby claims that

$$e^{3x} \geq e^{2x} \quad x \in \mathbb{R}$$

Determine whether Bobby's claim is always true, sometimes true or never true, justifying your answer.

(2)

(iii) Elsa claims that

‘for $n \in \mathbb{Z}^+$, if n^2 is even, then n must be even’

Use proof by contradiction to show that Elsa's claim is true.

(2)

(iv) Ying claims that

‘the sum of two different irrational numbers is irrational’

Determine whether Ying's claim is always true, sometimes true or never true, justifying your answer.

(2)



Question 8 continued

Handwriting practice area with 20 horizontal lines.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



S 6 3 4 4 8 A 0 2 3 4 8

Question 8 continued

Lined area for writing the answer to Question 8.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Question 8 continued

Handwriting practice area with 20 horizontal lines.

(Total for Question 8 is 8 marks)



9. (a) Show that

$$\frac{\sin x}{1 - \cos x} + \frac{1 - \cos x}{\sin x} \equiv k \operatorname{cosec} x \quad x \neq n\pi, \quad n \in \mathbb{Z}$$

where k is a constant to be found.

(4)

(b) Hence explain why the equation

$$\frac{\sin x}{1 - \cos x} + \frac{1 - \cos x}{\sin x} = 1.6$$

has no real solutions.

(1)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Question 9 continued

Lined area for writing the answer to Question 9.

(Total for Question 9 is 5 marks)



DO NOT WRITE IN THIS AREA



DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

- DO NOT WRITE IN THIS AREA**

DO NOT WRITE IN THIS AREA

- DO NOT WRITE IN THIS AREA**

DO NOT WRITE IN THIS AREA

Question 10 continued

Handwriting practice area with 20 horizontal lines.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



S 6 3 4 4 8 A 0 2 9 4 8

Question 10 continued

Lined area for writing the answer to Question 10.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Question 10 continued

Handwriting practice area with 20 horizontal lines.

(Total for Question 10 is 9 marks)



11. (i) Given that

$$y = a^x$$

where a is a positive constant, show that

$$\frac{dy}{dx} = a^x \ln a \quad (2)$$

(ii) Given that

$$x = 2 \tan y \quad -\frac{\pi}{2} < y < \frac{\pi}{2}$$

show that

$$\frac{dy}{dx} = \frac{k}{4 + x^2} \quad (4)$$

where k is a constant to be found.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Question 11 continued

Lined area for writing the answer to Question 11.

(Total for Question 11 is 6 marks)



12.

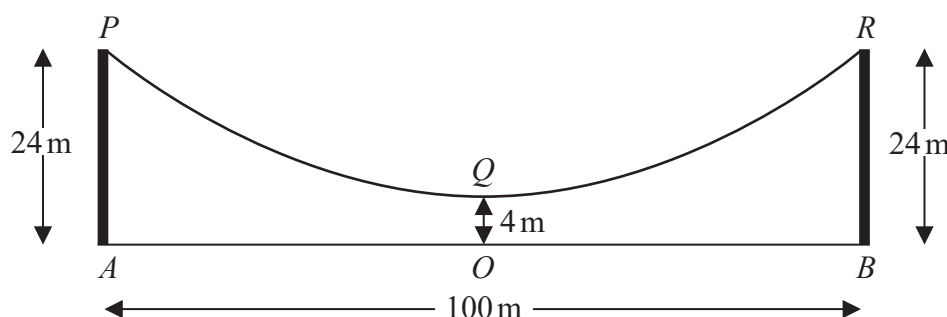


Figure 5

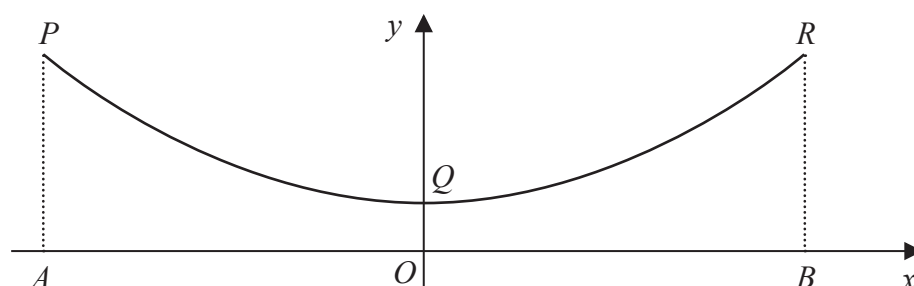


Figure 6

A suspension bridge cable PQR hangs between the tops of two vertical towers, AP and BR , as shown in Figure 5.

A walkway AOB runs between the bases of the towers, directly under the cable.

The towers are 100 m apart and each tower is 24 m high.

At the point O , midway between the towers, the cable is 4 m above the walkway.

The points P , Q , R , A , O and B are assumed to lie in the same vertical plane and AOB is assumed to be horizontal.

Figure 6 shows a symmetric quadratic curve PQR used to model this cable.

Given that O is the origin,

- (a) find an equation for the curve PQR . (3)

Lee can safely inspect the cable up to a height of 12 m above the walkway.

A defect is reported on the cable at a location 19 m horizontally **from one of the towers**.

- (b) Determine whether, according to the model, Lee can safely inspect this defect. (2)

- (c) Give a reason why this model may not be suitable to determine whether Lee can safely inspect this defect. (1)



Question 12 continued

Handwriting practice area with 30 horizontal lines.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Question 12 continued

Lined area for writing the answer to Question 12.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Question 12 continued

Handwriting practice area with 24 horizontal lines.

(Total for Question 12 is 6 marks)



13. Given that p is a positive constant,

(a) show that

$$\sum_{n=1}^{11} \ln(p^n) = k \ln p$$

where k is a constant to be found,

(2)

(b) show that

$$\sum_{n=1}^{11} \ln(8p^n) = 33 \ln(2p^2)$$

(2)

(c) Hence find the set of values of p for which

$$\sum_{n=1}^{11} \ln(8p^n) < 0$$

giving your answer in set notation.

(2)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Question 13 continued

Handwriting practice area with 20 horizontal lines.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Question 13 continued

Handwriting practice area with 25 horizontal lines.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Question 13 continued

Handwriting practice area with 28 horizontal lines.

(Total for Question 13 is 6 marks)



DO NOT WRITE IN THIS AREA



DO NOT WRITE IN THIS AREA

DON'T WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

Question 14 continued

Lined area for writing the answer to Question 14.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



S 6 3 4 4 8 A 0 4 3 4 8

Question 14 continued

Lined area for writing the answer to Question 14.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Question 14 continued

Handwriting practice area with 30 horizontal lines.

(Total for Question 14 is 10 marks)



DO NOT WRITE IN THIS AREA

DONOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DON'T WRITE IN THIS AREA

- (1)

DO NOT WRITE IN THIS AREA

- (4)

Question 15 continued

Handwriting practice area with 25 horizontal lines.

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



Question 15 continued

Lined area for writing answers to Question 15.

(Total for Question 15 is 5 marks)

TOTAL FOR PAPER IS 100 MARKS

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

