

**Y9 Unit 10 MARKSCHEME (total 30)**

**1 a** False – find a counter example e.g.  $4 > 3$  but  $-4$  is not bigger than  $-3$  **1 mark**

**b** False – find a counter example e.g. draw a rhombus showing 2 lines of symmetry **1 mark**

**2**  $2n$  is always even as  $2 \times$  any INTEGER is always even **1 mark**

and  $2n$  (even) + 10 (even) is always even. **1 mark**

**3 a** Yes,  $5 \times$  any number is in the 5 times table and is always a multiple of 5 because 5 will divide into it exactly. E.g. if  $x = 4$ ,  $5x = 20$  and 20 is a multiple of 5 because  $20 \div 5 = 4$ , where we started. **1 mark**

**b** No, use a counter example: if  $x = 3$ ,  $5x = 15$  which is not a multiple of 10

**OR** if  $x$  is even,  $5x$  is a multiple of 10 but if  $x$  is odd the  $5x$  ends in 5 and is not a multiple of 10.

**1 mark**

**4**

|                               | Example 1     | Example 2     | Algebra                                 |
|-------------------------------|---------------|---------------|-----------------------------------------|
| Think of a number             | e.g. 2        | e.g. 23       | $n$                                     |
| Multiply it by 2              | 4             | 46            | $2n$                                    |
| Add 9                         | 13            | 55            | $2n + 9$                                |
| Add your original number      | 15            | 78            | $3n + 9$                                |
| Divide by 3                   | 5             | 26            | $n + 3$                                 |
| Add 4                         | 9             | 30            | $n + 7$                                 |
| Subtract your original number | 7             | 7             | 7                                       |
| What is your result?          | 7             | 7             | 7                                       |
|                               | <b>1 mark</b> | <b>1 mark</b> | <b>2 marks</b> (minus 1 for each error) |

**5 a**  $5x = 5(x - 1) + 4$

$5x = 5x - 5 + 4$  **1 mark**

$5x = 5x - 1 \rightarrow$  NEVER TRUE **1 mark**

**b**  $(x + 2)^2 = x^2 + 4x + 4$   
 LHS =  $(x + 2)(x + 2)$   
 =  $x^2 + 2x + 2x + 4$  **1 mark**  
 =  $x^2 + 4x + 4$   
 = RHS → ALWAYS TRUE **1 mark**

**c**  $6x = 5x + 1$   
 subtract  $5x \dots$   $x = 1$  **1 mark**  
 SOMETIMES TRUE **1 mark**

**6** In triangle ABC and in triangle CDE:  
 angle BAC =  $40^\circ$  and angle CDE =  $40^\circ$  (alternate angles on parallel lines) **1 mark**  
 angle ABC =  $60^\circ$  and angle CED =  $60^\circ$  (alternate angles on parallel lines) **1 mark**  
 angle ACB =  $80^\circ$  and angle DCE =  $80^\circ$  (angles in a triangle add up to  $180^\circ$ ) **1 mark**  
 So the triangles have 3 equal angles  
 $\therefore$  triangle ABC is similar to triangle CDE **1 mark**

**7 a** Either  $2k - 1$  or  $2k + 3$  **1 mark**

|                                |                                |               |
|--------------------------------|--------------------------------|---------------|
| <b>b</b> For $2k - 1$ :        | Or for $2k + 3$ :              |               |
| Sum = $2k - 1 + 2k + 1$        | Sum = $2k + 3 + 2k + 1$        | <b>1 mark</b> |
| = $4k$                         | = $4k + 4$                     | <b>1 mark</b> |
| = $4 \times k$                 | = $4 \times (k + 1)$           |               |
| This is always a multiple of 4 | This is always a multiple of 4 | <b>1 mark</b> |

|                                      |                                      |               |
|--------------------------------------|--------------------------------------|---------------|
| <b>c</b> For $2k - 1$ :              | Or for $2k + 3$ :                    |               |
| Product = $(2k - 1)(2k + 1)$         | Product = $(2k + 3)(2k + 1)$         | <b>1 mark</b> |
| = $4k^2 - 1$                         | = $4k^2 + 8k + 3$                    | <b>1 mark</b> |
|                                      | = $4 \times (k^2 + 2k) + 3$          |               |
| = multiple of 4 minus 1              | = multiple of 4 add 3                |               |
| Which is 1 less than a multiple of 4 | Which is 1 less than a multiple of 4 | <b>1 mark</b> |

**8**

| Working                                                                                                      | Answer | Mark | Notes                                                                                                                                                                                                                                                                                     |
|--------------------------------------------------------------------------------------------------------------|--------|------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| $4n^2 + 12n + 3^2 - (4n^2 - 12n + 3^2)$<br>$= 4n^2 + 12n + 9 - 4n^2 + 12n - 9$<br>$= 24n$<br>$= 8 \times 3n$ | Proof  | 3    | M1 for 3 out of 4 terms correct in expansion of either $(2n + 3)^2$ or $(2n - 3)^2$<br>or $((2n + 3) - (2n - 3))((2n + 3) + (2n - 3))$<br>A1 for $24n$ from correct expansion of both brackets<br>A1 (dep on A1) for $24n$ is a multiple of 8 or $24n = 8 \times 3n$ or $24n \div 8 = 3n$ |